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for circular orbit  $e = 1$

$$e = \frac{Ch^2}{GM_e}$$

in this case we have Mars.

$$M_e \rightarrow M_{\text{mars}} = 0.1074 M_e$$

$$1 = \frac{Ch^2}{GM_e}$$

$$66.73 \times 10^{-12} / 0.1074 (5.976 \times 10^{24})$$

For parabolic orbit

$$V_e = \sqrt{\frac{2GM_{\text{mars}}}{r_0}}$$

$$\frac{10 \times 10^6}{3600} = \sqrt{\frac{2(66.73 \times 10^{-12})(0.1074 \times 5.976 \times 10^{24})}{r_0}}$$

$$\Rightarrow r_0 =$$

now at  $r_0$ , spacecraft is injected into circular orbit

$$V_c = \sqrt{\frac{GM_{\text{mars}}}{r_0}}$$

$$= \sqrt{\frac{(66.73 \times 10^{-12})(0.1074 \times 5.976 \times 10^{24})}{r_0}}$$

$$V_c =$$

This is the velocity that must be implemented at  $r_0$  from Mars and maintained to have a circular orbit. In practise how would you do this.

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$r_0 = r_p = 4000 \text{ mi} = (4000)(5280) \text{ ft.}$   
 So we need free flight speed at perigee  
 (-or periapsis)

$$r_a = \frac{r_0}{\frac{2GM_e}{r_0 V_0^2} - 1} = \frac{r_p}{\frac{2G(0.6M_e)}{r_p V_p^2} - 1}$$

$$V_p = \left\{ \left( \frac{r_p}{r_a} + 1 \right) \left[ \frac{r_p}{2G(0.6M_e)} \right] \right\}^{-1/2}$$

$$V_p = \left( \frac{4000}{10000} + 1 \right) \left[ \frac{4000(5280)}{2(34.4 \times 10^{-9})(0.6)(409 \times 10^{21})} \right]^{-1/2}$$

$$= \text{ft/s.}$$

13-123

To find free-flight speed at apoapsis, same process  
 as above, but  $r_0 = r_p = 2000 \text{ mi}$

- Next  $V_p$

- Next: from eccentricity formula

$$h = r_0 V_0 = r_p V_p = r_a V_a$$

so we get  $V_a$  or speed at  $A'$

Time elapsed from A' to B ?

we have constant acceleration because we are in free flight.

Students see how you can use Equations of motion to figure this out.

Alternately we can use the Period T formula. T is the time for 1 orbit. From

$$T = \frac{\pi}{h} (r_p + r_a) \sqrt{r_p r_a}$$

from A' to B is half of an orbit

$$\frac{T}{2} = \frac{\pi}{2h} (r_p + r_a) \sqrt{r_p r_a}$$

In general to find time to some point of an ellipse, find the corresponding area and its proportion with regard to total ellipse area, then adjust the period T formula accordingly.

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$$V_p = 25 \text{ Mm/h}$$

$$r_p = ?$$

$$V_a = 15 \text{ Mm/h}$$

$$r_a = 6378 \text{ Km} + 18 \text{ Mm}$$

$$= 24.378 \text{ Mm}$$

$$h = r_p V_p = r_a V_a$$

$$25 r_p = 24.378 (15) =$$

$$r_p = \text{Mm}$$

$$\text{Period, } T = \frac{\pi}{h} (r_p + r_a) \sqrt{r_p r_a}$$

from our data, answer will be in hours.